

FORMULAS

Bivariate regression models

$$E(y) = \alpha + \beta x \quad \hat{y} = a + bx \quad r = b(s_x/s_y) \quad r^2 = (TSS - SSE)/(TSS)$$

$$b \pm t(se) \quad t = \frac{b}{se} \quad (df = n - 2), \quad se = \frac{s}{\sqrt{\sum(x - \bar{x})^2}} = \frac{s}{s_x \sqrt{n - 1}} \quad s = \sqrt{\frac{SSE}{(n - 2)}}$$

$$s = \sqrt{SSE/(n - 2)} = \text{Root MSE}$$

Multiple regression models

$$E(y) = \alpha + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k \quad \hat{y} = a + b_1 x_1 + b_2 x_2 + \cdots + b_k x_k$$

$$R^2 = (TSS - SSE)/(TSS) \quad TSS = \sum(y - \bar{y})^2 \quad SSE = \sum(y - \hat{y})^2$$

$$F = \frac{R^2/k}{(1 - R^2)/[n - (k + 1)]} = \frac{\text{MS(regression)}}{\text{MSE}} \quad df_1 = k, \quad df_2 = n - (k + 1)$$

$$t = b_i/se \quad df = n - (k + 1) \quad b_i \pm t_{\alpha/2}(se)$$

Comparing models:

$$F = \frac{(R_c^2 - R_r^2)/df_1}{(1 - R_c^2)/df_2}, \quad df_1 = \text{no. extra parameters}, \quad df_2 = n - (k + 1) \quad \text{complete model}$$